

# My Experience as a (Not-So-Young) Post-Doc in Nuclear Theory

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# What makes Nuclear Theory interesting? [A subjective take]

The **Nuclear Interaction** comes from **Quantum Chromodynamics (QCD)**.

However, with our current computational capabilities,  
we cannot even describe fully all the properties of the proton.

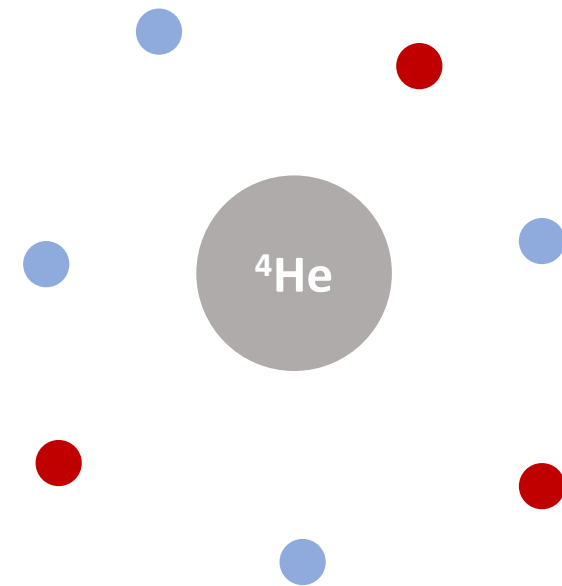
As a result, **all nuclear models are phenomenological** (parameter fitting),  
with different levels of phenomenology, leaving the place  
to **all different kinds of Physics within Nuclear Theory**.

In this presentation, I will share some of my **personal experience**  
with the different aspects of Physics within Nuclear Theory,  
highlighting the **diversity of the field**.

# Shell Model (embedded in the continuum)

- ▶ Model = an **inert core** + **valence nucleons**

$$\mathcal{H} = \sum_{i=1}^{N_{val}} \left[ \frac{\vec{p}_i^2}{2\mu_i} + U(i) \right] + \sum_{i < j=1}^{N_{val}} V_{res}(i,j) + \dots$$

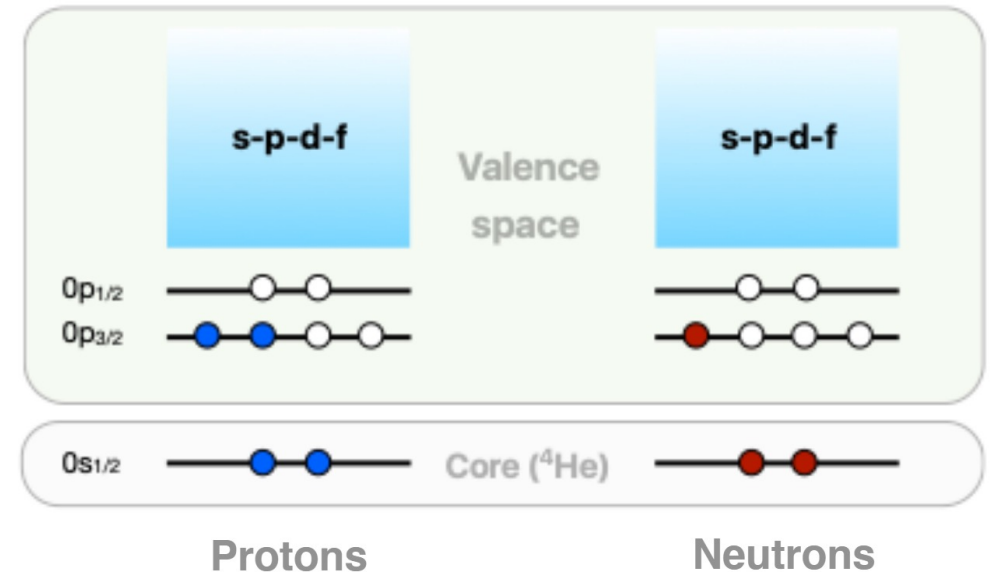


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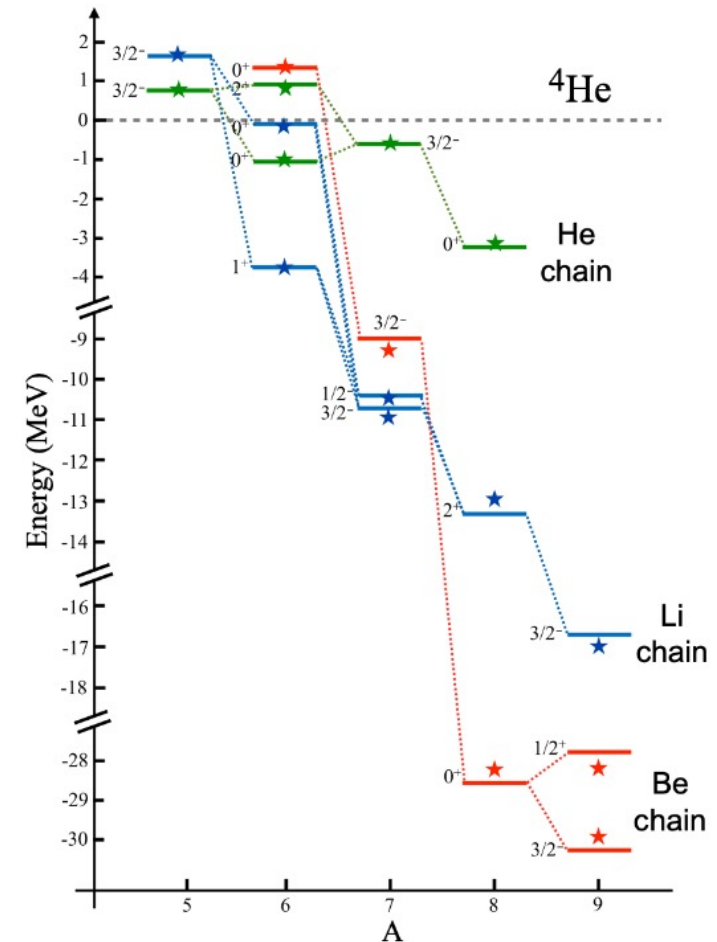
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- ▶  $U$  generates the **shells [basis]**.  $U$  and  $V_{res}$  can come from:
  - **First principles** (Ab Initio No Core Shell Model)
  - **Effective forms** (analytical formulas etc.).
- ▶ The **Gamow Shell Model** is an extension of the Shell Model in the **continuum** [particle emission].
- ▶ Diagonalization of  $\mathcal{H}$  gives the  $A$ -body nuclear states.



# Shell Model (embedded in the continuum)

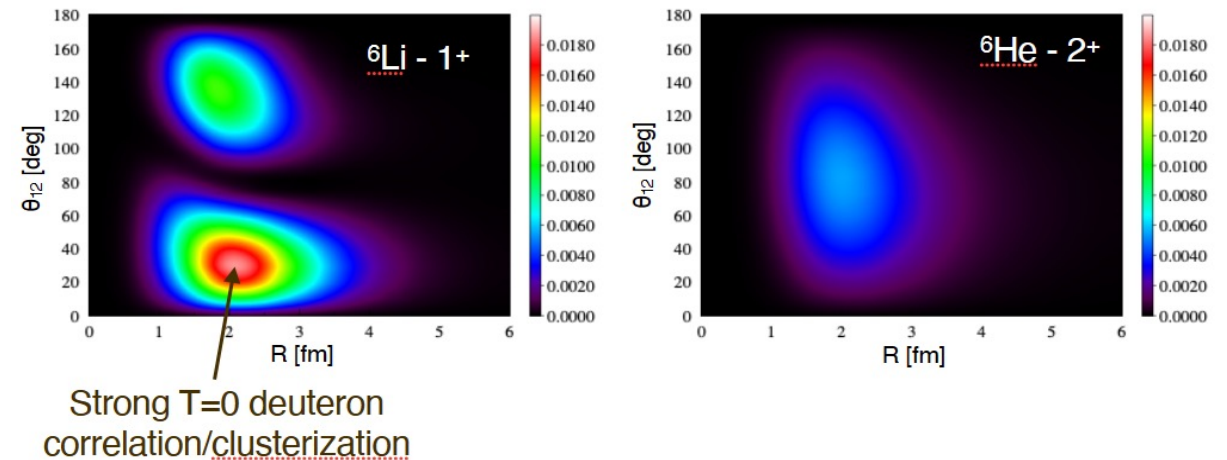
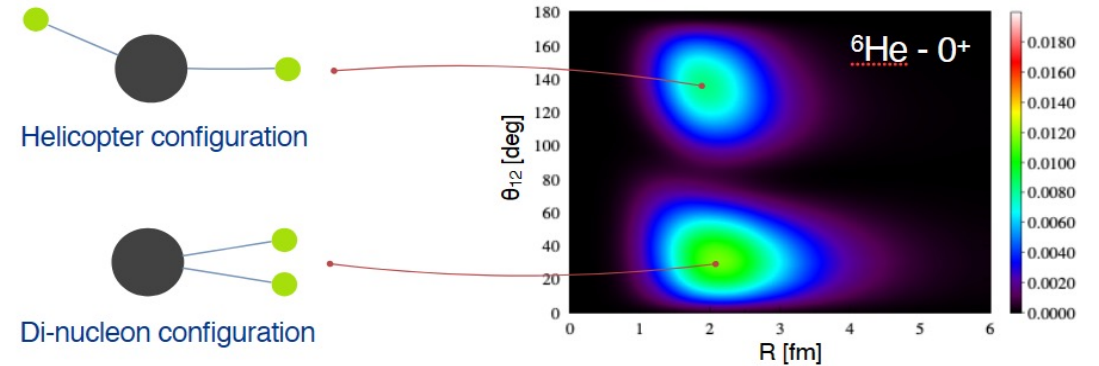
- ▶ An interaction with **spin-orbit, tensor and Coulomb** to describe the whole **psd-shell** nuclei ( $A = 5 - 15$ ).  
For **bound states and resonances**.  
With **uncertainty quantification**.



Y.J. *et al.*, Phys. Rev. C 96, 054316 (2017)

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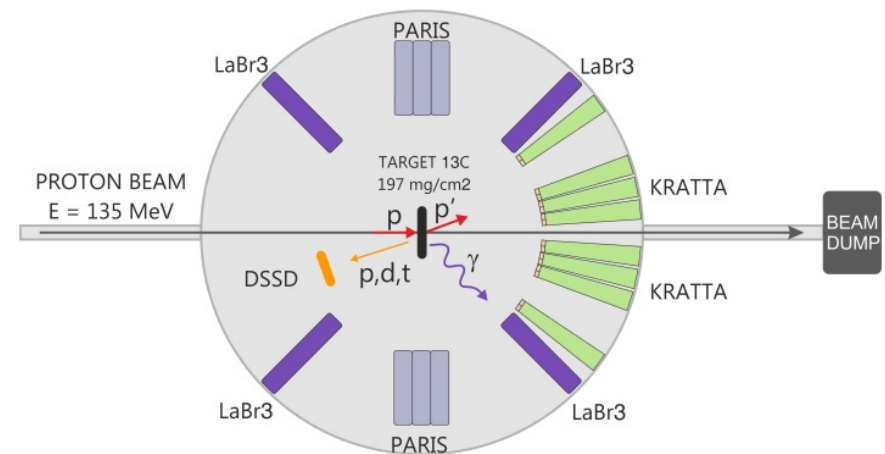
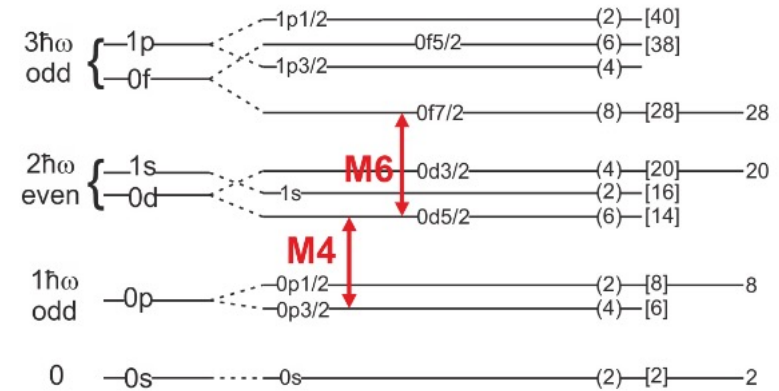
- ▶ An interaction with **spin-orbit, tensor and Coulomb** to describe the whole **psd-shell** nuclei ( $A = 5 - 15$ ).  
For **bound states and resonances**.  
With **uncertainty quantification**.
- ▶ Description of exotic phenomena:
  - **Halo states**
  - **Helicopter/di-nucleon configuration**
  - **Deuteron clusterization...**



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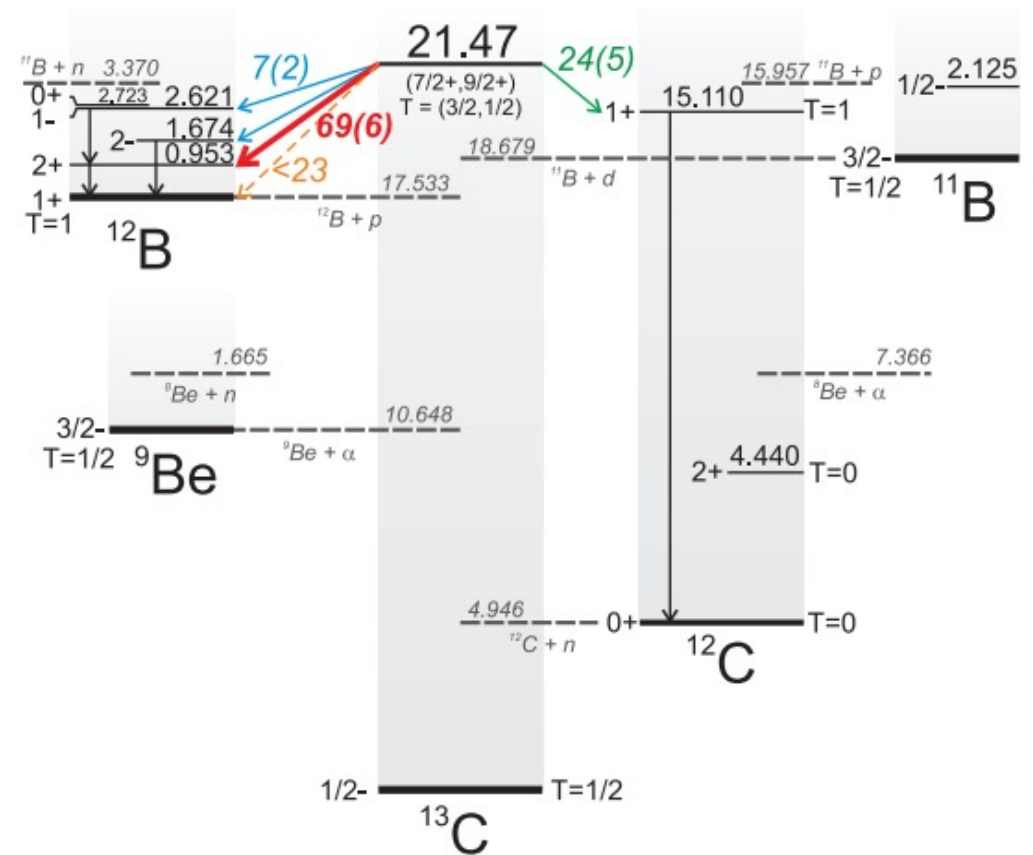
# Super-stretched states (direct collaboration with experimentalists)

- ▶ Existence of a **M4 super-stretched** state in  $^{13}\text{C}$ .  
(Almost) pure neutron excitation from  $0p_{3/2}$  to  $0d_{5/2}$   
Gives precise information on the nuclear interaction.
- ▶ In **collaboration with experimentalists** from Kraków  
Experience performed at the **Cyclotron Centre Bronowice**  
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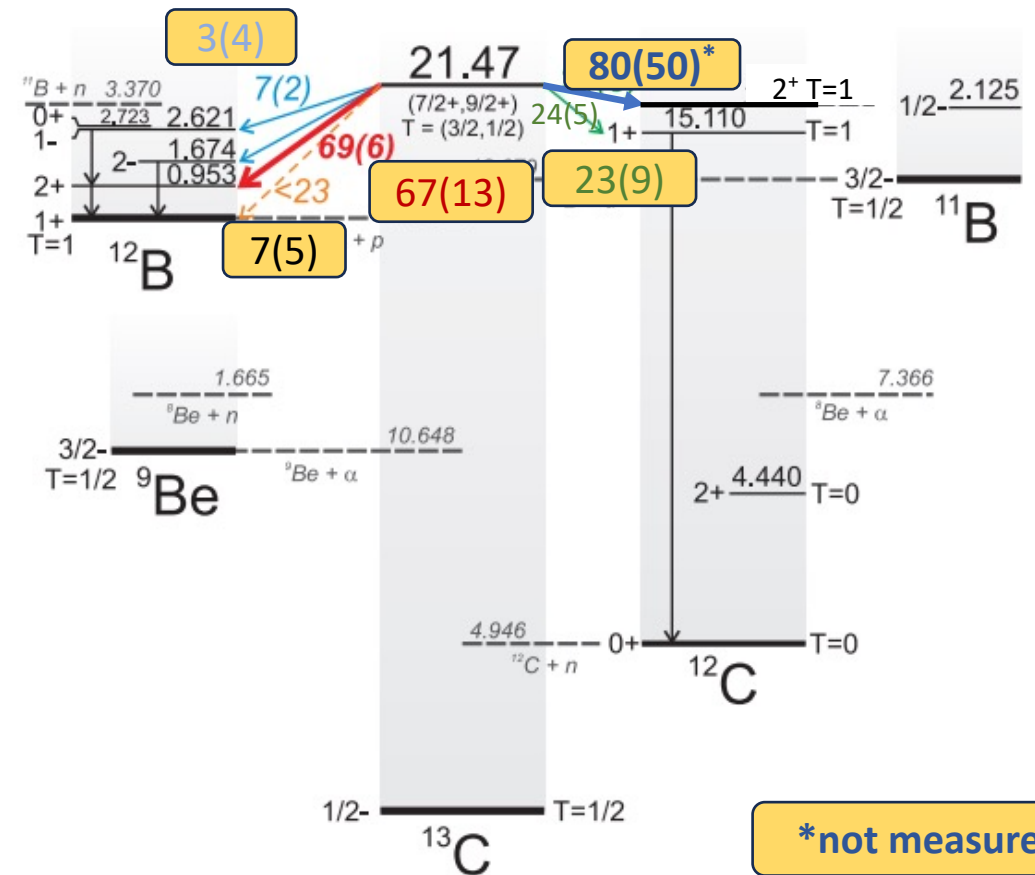


N. Cieplicka, Y. J. *et al.*, Phys. Lett. B 834, 137398 (2022)



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- ▶ **Fine-tuning** of the previous interaction to the  
neighboring states/nuclei.
- ▶ **High phenomenology** is often required to describe  
**experimental data** with an acceptable precision.



N. Cieplicka, Y. J. *et al.*, Phys. Lett. B 834, 137398 (2022)

# Self-consistent calculations / Genuine ternary fission

- ▶ In the **Hartree-Fock + BCS method**, the nuclear states are obtained by minimizing the Routhian:

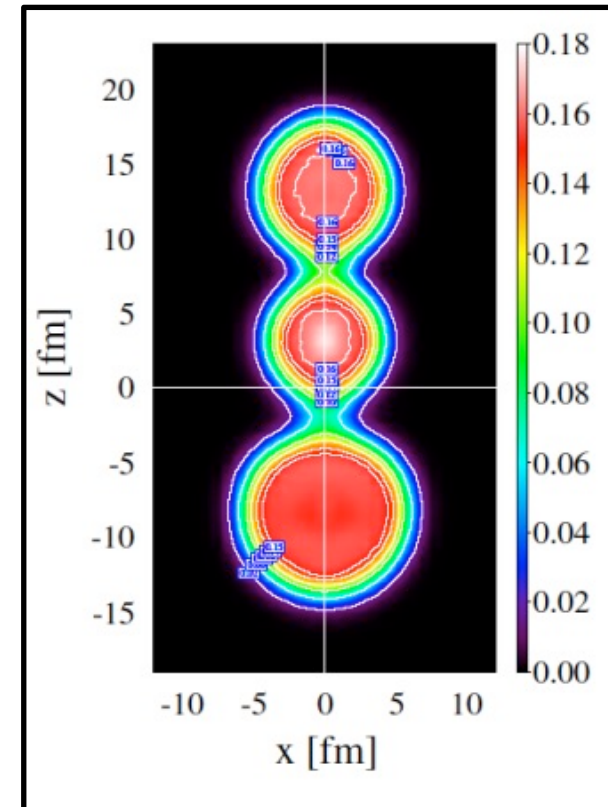
$$\delta \left( \left\langle \phi \left| \hat{H} - \sum_i \lambda_i \hat{Q}_i - \lambda_N \hat{N} - \lambda_Z \hat{Z} \right| \phi \right\rangle \right) = 0$$

with the **constraints**  $\langle \phi | \hat{Q} | \phi \rangle = Q_{constr}$  (quadrupole moment etc.)

- ▶ One obtains the **ground states** and **some excited states**.
- ▶ **Possibilities to go beyond mean-field to compute the whole spectrum.**

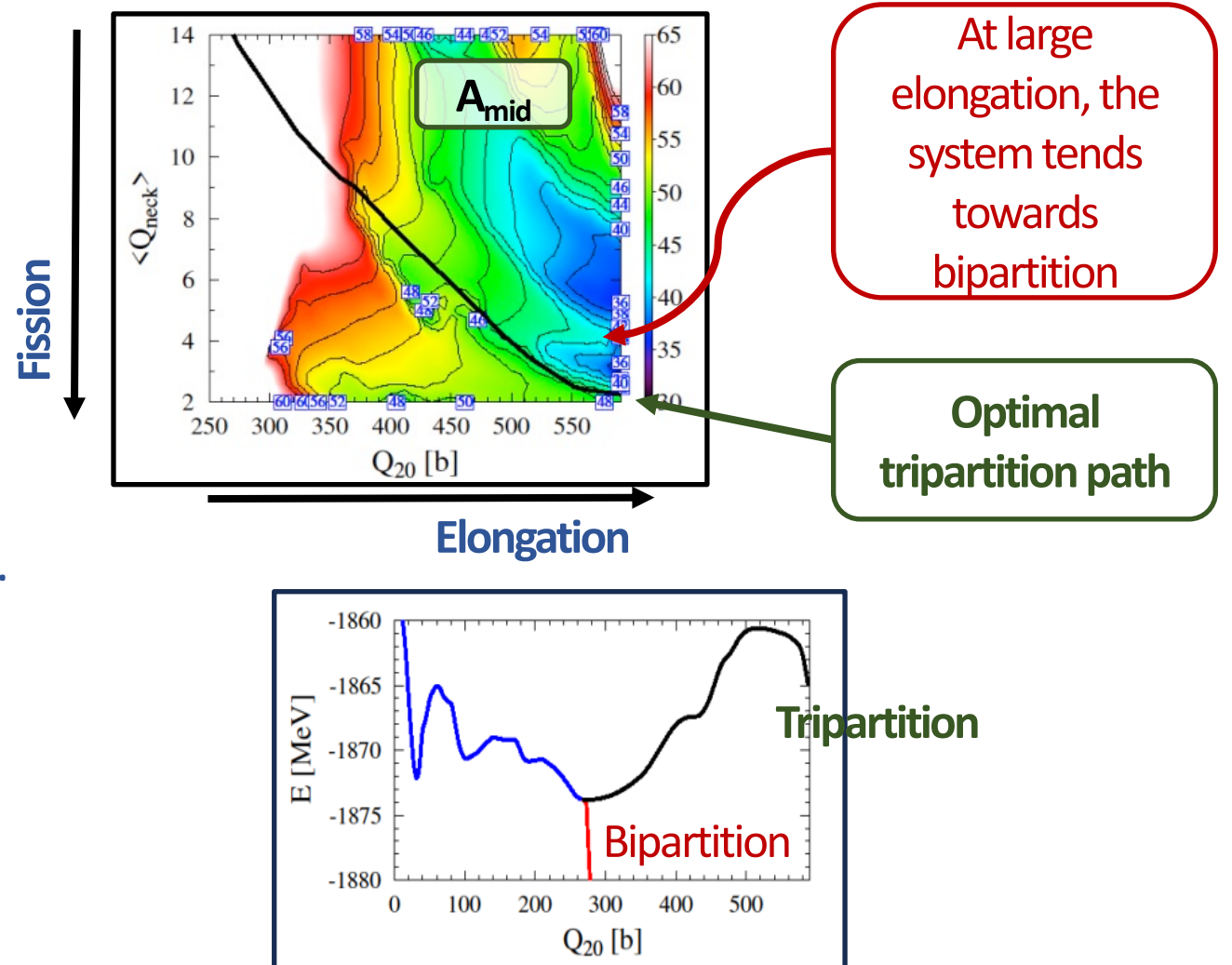
# Self-consistent calculations / Genuine ternary fission

- ▶ A question out of curiosity...
- ▶ **Genuine ternary fission** is an extremely rare process.
- ▶ Generally, the additional fragment is an  $\alpha$ -particle.
- ▶ The existence of genuine **ternary fission with a heavier fragment** is still an open question.
- ▶ Actinides:  ${}^{252}_{98}\text{Cf} \rightarrow {}^{132}_{50}\text{Sn}_{82} + {}^{48}_{20}\text{Ca}_{28} + {}^{72}_{28}\text{Ni}_{44}$
- ▶ **Experimental hints** to a colinear tripartition fission.
- ▶ HF + BCS calculations with **neck constraints**.



# Self-consistent calculations / Genuine ternary fission

- ▶ With neck constraints properly chosen for  $^{48}\text{Ca}$  as the middle fragment, one sees a **potential path to tripartition**.
- ▶ **Tripartition possible with a barrier of  $\sim 13\text{MeV}$ .**
- ▶ **Impossible paths for other partitions ( $^{40}\text{S}$ ).**



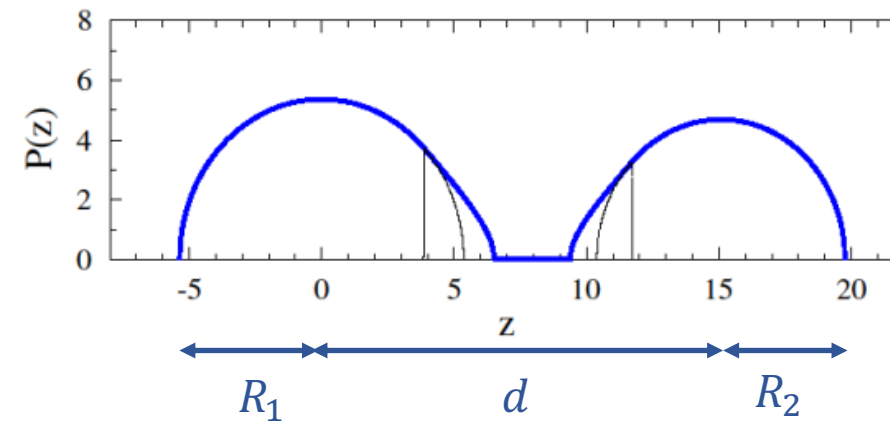
Y.J., J. Skalski, in preparation

# Dissipative dynamics / Fusion in the Langevin formalism

- ▶ Axially symmetric **parameterized** shapes.
- ▶ **Spherical** cups connected by quadratic surfaces<sup>[1]</sup>
- ▶ **Three shape variables:**
  - ▶ Distance/elongation  $\rho$
  - ▶ Neck/deformation  $\lambda$
  - ▶ **Asymmetry**  $\Delta$
- ▶ Three angular variables:
  - ▶ For a correct description of angular momentum

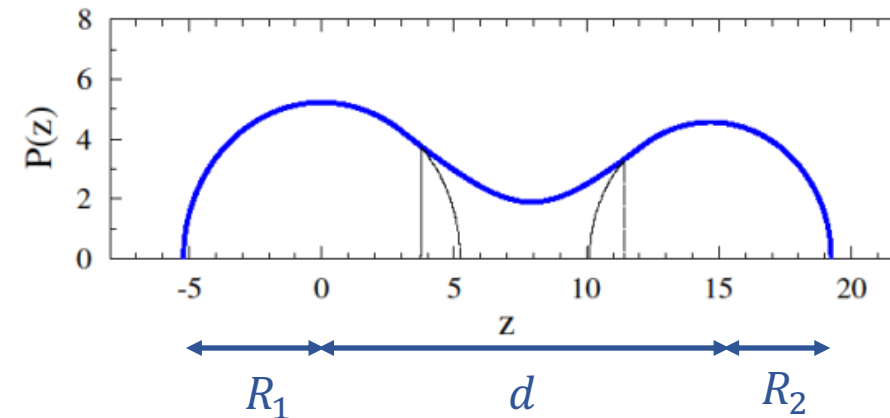
[1] J. Błocki, H. Feldmeier and W. J. Świątecki, Nucl. Phys. A 459 (1986) 145

$^{92}\text{Zr} + ^{64}\text{Ni}$



**Bipartite**

$$\begin{aligned}\rho &= 1.5 \\ \lambda &= 0.3 \\ \Delta &= \Delta_0\end{aligned}$$



**Monopartite**

$$\begin{aligned}\rho &= 1.5 \\ \lambda &= 0.4 \\ \Delta &= \Delta_0\end{aligned}$$

# Dissipative dynamics / Fusion in the Langevin formalism

- ▶ The **collective variables**  $q_i(t)$  and their **associated moments**  $p_i(t)$  follow the **Langevin equations**:

$$\dot{q}_i(t) = \sum_k (\mathcal{M}^{-1})_{ik} p_k \quad \Leftrightarrow (P = MV)$$

$$\dot{p}_i(t) = -\frac{\partial H}{\partial q_i} - \sum_k \gamma_{ik} \dot{q}_k + \sum_k g_{ik} \xi_k(t) \quad \Leftrightarrow \left( \frac{dP}{dt} = \Sigma F \right)$$

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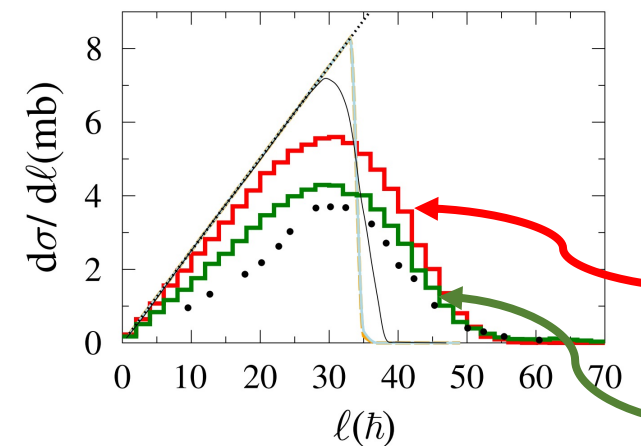
**Conservative forces**  
 $H = T + V$ ,  $V$  can be macroscopic or  
microscopic (shell corrections)

**Langevin/random forces**  
(quantum origin)

→ A comprehensive understanding of the dynamics process.

# Dissipative dynamics / Fusion in the Langevin formalism

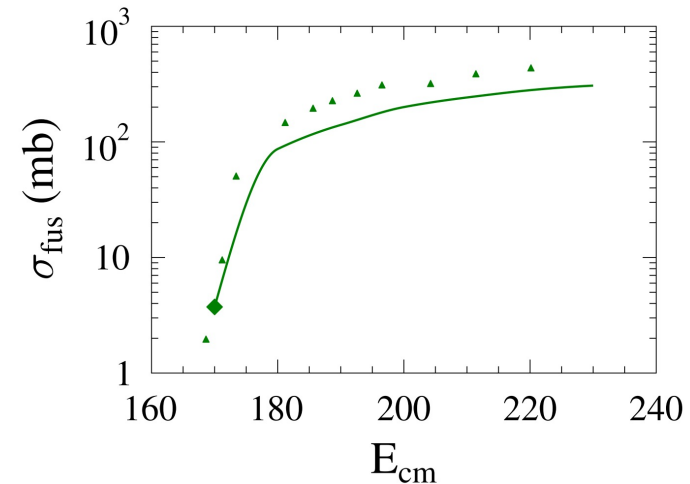
- ▶ Experimental data are well reproduced with a simple Yukawa-plus-exponential folding potential + Coulomb macroscopic potential.
- ▶ **No parameters adjusted to our calculations!**
- ▶ Upcoming calculations involving heavier systems ( $^{50}\text{Ti}$ ,  $^{54}\text{Cr}$ ) to study the hindrance mechanism, which prevents the formation of super-heavy nuclei.



Spin distribution of  
 $^{64}\text{Ni} + ^{92}\text{Zr} \rightarrow ^{156}\text{Er}$   
at  $E_{\text{cm}} = 138.8 \text{ MeV}$

Asymmetry fixed

Free asymmetry



Excitation function of  
 $^{48}\text{Ca} + ^{208}\text{Pb} \rightarrow ^{256}\text{No}$

Y. J., M. Kowal *et al.* in preparation



# Conclusions and perspectives

- ▶ **Nuclear Theory** is an **extremely diverse field**, encompassing different types of Physics.
- ▶ **All nuclear models are phenomenological**, with the level of phenomenology depending on the Physics they are aiming to explain.
- ▶ Many open problems persist in Nuclear Theory, with **potential solutions increasingly attainable thanks to advances in supercomputing**.

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Dziękuję za  
państwa uwagę!